Large-Signal Transient Analysis of Forward Converter with Active-Clamp Reset

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Abstract -- The forward converter with the active-clamp reset offers many advantages over the forward converter with other transformer reset methods. However, during the line and load transients, the maximum magnetizing current of the transformer and the peak voltage of the primary switch are strongly affected by the active-clamp circuit dynamics. As a result, the design of a forward converter with the active-clamp reset cannot be optimized based only on its dc characteristics. In this paper, a large-signal analysis of the forward converter with the active-clamp reset and output-voltage feedback control is presented. The analysis can be used to predict converter's dynamic performance.

I. INTRODUCTION

The forward converter is one of the most popular switching topologies for low and medium power applications. To achieve high efficiency at higher switching frequencies, an active-clamp reset circuit is often applied across the main switch [1]. The function of the active-clamp reset circuit is to provide the flux reset of the core of the power transformer, thus eliminating the need for additional winding or a dissipative RCD-clamp reset. A number of papers have discussed many design issues which relate to the active-clamp reset mechanism [2-6], but no explicit analysis has been presented so far for the large signal transient response. Since during large-signal transients, the active-clamp-circuit dynamics strongly affects the maximum magnetizing current of the transformer and the peak voltage of the primary switch, the design of a forward converter with the active-clamp reset cannot be optimized based only on its dc characteristics.

In this paper, an average state trajectory approach is used to analyze the response of the active-clamp circuit with output-voltage feedback control during line and load transients. It is shown that in addition to the selection of transformer parameters and the active-clamp capacitance, the control loop bandwidth is a design parameter which determines the maximum voltage of the main power switch and magnetizing current of the transformer during transients.

II. LARGE-SIGNAL TRANSIENT BEHAVIOR

The forward converter power-stage with the active-clamp reset is shown in Fig. 1. The active-clamp reset circuit consists of the series connection of auxiliary switch S₂ and clamp capacitor Cₖ. It should be noted that transformer in Fig. 1 is shown as a parallel connection of the magnetizing inductance Lₘ and the ideal transformer with a turns-ratio n = Nₕ / Nₛ.

\[
\begin{align*}
V_{\text{m}} &\rightarrow V_C \rightarrow L_M \rightarrow I_M \rightarrow D_1 \rightarrow L_F \rightarrow V_D \\
N_h &\rightarrow N_s \rightarrow D_2 \rightarrow L_p \rightarrow V_S \\
S_1 &\rightarrow S_2 \rightarrow + V_S \\
\end{align*}
\]

Fig. 1. Active-clamp forward converter circuit diagram.

To illustrate the behavior of the forward converter with active-clamp reset, Fig. 2 shows the simulation results of the circuit in Fig. 1 with output-voltage feedback control during large-signal transients. Fig. 2(a) shows clamp-capacitor voltage Vₖ, magnetizing current of the transformer Iₘ, and output voltage of the error amplifier Vₑ during an input-voltage transient from 100 V to 200 V. Fig. 2(b) shows the same waveforms during a load transient from 18 A to 20 A. The circuit parameters used in the simulations using SIMPLIS simulation software [7] are: Lₘ=2.5 mH, Cₖ=22 nF, maximum duty cycle Dₘ₉=0.7, switching frequency fₛ=100 kHz, and control loop crossover frequency f₉=3.6 kHz.

As can be seen from Fig. 2(a) and (b), the peak voltage of the clamp voltage and magnetizing current during transients are much larger than the ripple voltage and current in steady state. Therefore, for a proper design of the circuit, it is very important to understand the circuit performance and predict the maximum stresses of the components during large-signal transients.

Specifically, before the input-voltage transient, the converter in Fig. 2(a) operates with a large duty cycle and with a balanced flux in the core so that \( V_{\text{IN}} \cdot D = V_C \cdot (1-D) \). Since after the line change, the duty cycle and the clamp-capacitor voltage Vₖ does not change instantaneously, the volt-second product becomes unbalanced, i.e., \( V_{\text{IN}} \cdot D > V_C \cdot (1-D) \). As a result, the magnetizing current of the transformer starts increasing after the input-voltage change. The increased magnetizing energy charges the clamp capacitor, increasing the clamp-capacitor voltage. This transition continues until Vₖ becomes large enough so that the volt-second product becomes \( V_{\text{IN}} \cdot D < V_C \cdot (1-D) \), and
the magnetizing current of the transformer starts to decrease. The described clamp-capacitor voltage increase and the subsequent decrease after the transient can be seen as an oscillatory response of the resonant circuit consisting of the clamp capacitor and the magnetizing inductance of the transformer. Similar resonant behavior during load transient can be observed in Fig. 2(b).

If the forward converter circuit with the active-clamp reset is not correctly designed, the peak clamp-capacitor voltage and magnetizing current during input-voltage and load transients may cause an excessive voltage stress on the primary switch and/or saturation of the core of the transformer. Yet another problem that may happen during transients is that the body diode of auxiliary switch \( S_2 \) may conduct due to a positive magnetizing current at the instant when main switch \( S_1 \) is turned on, as indicated in Fig. 2(a). If the auxiliary-switch body diode is conducting when the main switch \( S_1 \) is turned on, a slow reverse-recovery of the body diode may cause the failure of the circuit because of the low-impedance current path through the clamp capacitor, the auxiliary-switch body diode, and the main switch [2].

![Graph](image)

**Fig. 2. Simulation results of large-signal transients of the forward converter with the active-clamp reset and output-voltage feedback control: (a) input-voltage step change from 100 V to 200 V; (b) load step change from 18 A to 20 A.**

One approach to eliminate this problem is to connect a Schottky diode in series with the auxiliary switch to block the conduction of the body diode, and then to connect a fast-recovery anti-parallel diode around the series connection of the Schottky and the auxiliary switch [2]. The other approach is to design an active-clamp circuit, so that the magnetizing current is always negative at the instant main switch \( S_1 \) is turned on.

### III. STATE TRAJECTORY OF ACTIVE-CLAMP RESET CIRCUIT

Fig. 3(a) and Fig. 3(b) are the simplified circuit diagrams during main switch \( S_1 \) turn-on and turn-off period, respectively. The state equations of \( v_c \) and \( i_m \) during \( S_1 \) on the period, Fig. 3(a), are

\[
C_C \cdot \frac{dv_c}{dt} = i_m \tag{1}
\]

\[
L_M \cdot \frac{di_m}{dt} = v_c \tag{2}
\]

By solving (1) and (2), the state trajectory during the on-time of \( S_1 \) can be described as

\[
v_c(t) = v_c(t_0) \tag{3}
\]

\[
i_m(t) = \frac{i_m(t_0)}{L_M} \cdot t + i_m(t_0) \tag{4}
\]

where \( v_c(t_0) \) is the initial value of the clamp-capacitor voltage and \( i_m(t_0) \) is the initial value of the magnetizing current of the transformer at the main-switch-on instant. The state trajectory during this period is a line parallel to \( i_m \) axis with a constant \( v_c \), as shown in Fig. 4.

During the off period, Fig. 3(b), the state equations of \( v_c \) and \( i_m \) are

\[
C_C \cdot \frac{dv_c}{dt} = i_m \tag{5}
\]

\[
L_M \cdot \frac{di_m}{dt} = -v_c \tag{6}
\]

By solving (5) and (6), the state trajectory during the off-time of \( S_1 \) can be described as

\[
v_c(t) = r \cdot \cos[a - \omega_o \cdot t] \tag{7}
\]

\[
i_m(t) \cdot Z_o = r \cdot \sin[a - \omega_o \cdot t] \tag{8}
\]

\[
v_c(t) + i_m(t) \cdot Z_o = r^2 \tag{9}
\]

where,

\[
r = \sqrt{v_c(t_0)^2 + i_m(t_0)^2 \cdot Z_o^2} \tag{10}
\]

\[
a = \tan^{-1} \left( \frac{i_m(t_0) \cdot Z_o}{v_c(t_0)} \right) \tag{11}
\]

\[
\omega_o = \frac{1}{\sqrt{L_M \cdot C_C}} \tag{12}
\]

\[
Z_o = \frac{L_M}{C_C} \tag{13}
\]

\( v_c(t_0) \) is the initial value of the clamp-capacitor voltage, and \( i_m(t_1) \) is the initial value of the magnetizing current of the transformer at the turn-off instant of main switch \( S_1 \). The state trajectory during this period is shown in Fig. 4.

The solid line in Fig. 5 shows the state trajectory of the active-clamp reset circuit during the same input-
voltage transient as in Fig. 2(a). The state trajectory starts with a closed cycle as described in Fig. 4. The dashed line in Fig. 5 shows the average-model state trajectory which has a simpler waveform than the state trajectory. The average state trajectory is going to be discussed later.

Fig. 3 Simplified circuit diagrams: (a) during the on period of main switch; (b) during the off period of main switch.

Fig. 4. The state trajectory of the active-clamp reset circuit in steady state.

The transient behavior of the active-clamp reset circuit depends on the speed of the control and the characteristics of the resonant circuit. As can be seen from Fig. 2(a) and Fig. 2(b), the clamp voltage and magnetizing current transient waveforms show a resonant behavior with superimposed high switching-frequency ripples. Usually the resonant frequency is at least one magnitude smaller than the switching frequency in order to obtain a small ripple voltage of the clamp capacitor in steady state. Therefore, to simplify the analysis, the switching frequency ripples are ignored in the following analysis. However, the clamp voltage and magnetizing current ripples can be easily added into the results obtained by the simplified model later. As an illustration, Fig. 5 shows the relationship between state trajectory (solid line) and average state trajectory (dashed line).

A. Average model of the active-clamp forward converter

From Fig. 3(a) and Fig. 3(b), by ignoring the high switching frequency ripples, the average model of the active-clamp forward converter can be written as

\[ C_f \frac{dv_c}{dt} = i_t + I_o - V_o, \]  
\[ L_f \frac{di_f}{dt} = \frac{d \cdot V_{in}}{n} - v_p, \]  
\[ L_m \frac{di_m}{dt} = d \cdot V_{in} - d \cdot v_c, \]  
\[ C_c \frac{dv_c}{dt} = d^2 i_n, \]  

where \( d \) is the duty cycle of main switch and \( d' = 1 - d \).

Equations (16) and (17) can be rewritten as

\[ \left( \frac{L_m}{d'} \right) \frac{di_m}{dt} = \frac{d}{d'} \cdot V_{in} - v_c, \]  
\[ \left( \frac{C_c}{d'} \right) \frac{dv_c}{dt} = i_n. \]  

According to Eqs.(14)-(19), the average model of the forward converter power stage and the active-clamp reset circuit can be drawn as in Fig. 6(a) and Fig. 6(b), respectively. As can be seen from Fig. 6, the forward converter power stage and the active-clamp reset circuit are only coupled through the duty cycle. For the step input-voltage and load changes, the forward converter power stage represents a linear system. However, the average active-clamp reset circuit is nonlinear with respect to the duty cycle.

Fig. 5 The state trajectory of the active-clamp reset circuit during input-voltage step from 100 V to 200 V transient.

IV. DUTY CYCLE EQUATIONS DURING STEP INPUT-VOLTAGE AND LOAD TRANSIENTS

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\[ L_m \frac{di_m}{dt} = d \cdot V_{in} - d \cdot v_c, \]  
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Fig. 6 The average model of the active-clamp forward converter: (a) average model of the forward converter power stage; (b) average model of the active-clamp reset circuit.
B. Duty cycle equations during line and load changes

To further study the transient behavior of the active-clamp circuit, it is necessary to know the duty cycle dependence during input-voltage and load changes. Assuming that the input-voltage perturbation is limited to a step change, and

$$V_{in\_new} = V_{in\_old} + \Delta V_{in}$$

$$I_{o\_new} = I_{o\_old} + \Delta I_o$$

$$D_{new} = D_{old} + \Delta d$$

$$V_{o\_new} = V_{o\_old} + \Delta V_o$$

where $\Delta V_{in}$ and $\Delta I_o$ are the perturbations and $\Delta d$ and $\Delta V_o$ are the corresponding deviations. The perturbations of (1) and (2) yield

$$\Delta V_o = G_v \cdot \Delta d + G_v \cdot \Delta V_{in} + Z_o \cdot \Delta I_o$$

where,

$$G_v = \frac{\Delta V_o}{\Delta V_{in}}$$ (22)

$$Z_o = \frac{\Delta V_o}{\Delta I_o}$$ (23)

$$G_d = \frac{\Delta V_o}{\Delta d}$$ (24)

Assuming the transfer function of control loop compensator is $A(s)$, the loop gain is $T(s) = A(s) \cdot G_d(s)$ as shown in the closed-loop block diagram of the forward converter in Fig. 7. According to Fig. 7, the closed loop equations are

$$\frac{\Delta d}{\Delta V_{in\_close}} = \frac{D_{old}}{V_{in\_new} \cdot 1+T(s)}$$ (25)

$$\frac{\Delta V_o}{\Delta I_o\_close} = \frac{D_{old} \cdot n}{V_{in\_new} \cdot 1+T(s)}$$ (26)

where, $D_{old}$ is the duty cycle before perturbation, and $V_{in\_new}$ is the input voltage after the line step change.

Generally, neglecting the ESR zero of output-filter capacitor $C_F$, the optimal compensation of the output-voltage feedback control loop requires the transfer function of the compensator in the form

$$A(s) = \frac{A_{dc}}{s} \cdot \frac{(1+\frac{s}{\omega_z})}{(1+\frac{s}{\omega_c})}$$ (27)

where, compensator zeroes $\omega_{z1}$ and $\omega_{z2}$ are placed to cancel two poles in $G_v$ transfer function, i.e., $\omega_{z1}$ and $\omega_{z2}$ are close to $\frac{1}{\sqrt{L_F \cdot C_F}}$, and $\omega_p$ is placed at a frequency between crossover frequency $\omega_c$ and switching frequency $\omega_s$ [8].

Since when $T \gg 1$, $\frac{T}{1+T} \approx 1$, and when $T \ll 1$,

$$\frac{T}{1+T} \approx T.$$ The transfer function becomes

$$\frac{T}{1+T} \approx \frac{1}{(1+\frac{s}{\omega_c}) \cdot (1+\frac{s}{\omega_p})},$$ (28)

as shown in Fig. 8.

Fig. 7 Forward converter closed loop block diagram.

Substituting (28) into (25) and (26), the closed-loop transfer functions are

$$\frac{\Delta d}{\Delta V_{in\_close}} = \frac{D_{old}}{V_{in\_new} \cdot (1+\frac{s}{\omega_c}) \cdot (1+\frac{s}{\omega_p})},$$ (29)

$$\frac{\Delta V_o}{\Delta I_o\_close} = \frac{s \cdot L_F \cdot n}{V_{in\_new} \cdot (1+\frac{s}{\omega_c}) \cdot (1+\frac{s}{\omega_p})}. $$ (30)

Therefore, from (29), for a step input voltage change, the time domain equation for the duty cycle can be written as

$$d(t) = D_{old} \cdot e^{-\frac{\omega_p}{\omega_c}} \cdot \omega_p \cdot e^{-\frac{\omega_p}{\omega_c}} \cdot e^{-\frac{\omega_p}{\omega_c}}$$ (31)

Because generally $\omega_p$ is selected so that $\omega_p \gg \omega_c$, (31) can be simplified to

$$d(t) = D_{old} + (D_{new} - D_{old}) \cdot (1 - e^{-\frac{\omega_p}{\omega_c}}).$$ (32)

Similarly, from Eq. (30), under the same assumptions, the time domain equation for the duty cycle during a step load change can be obtained as

$$d(t) = D_{old} - \frac{n \cdot \omega_p \cdot L_F \cdot \Delta I_o}{V_{in}} \cdot e^{-\frac{\omega_p}{\omega_c}}.$$ (33)

V. LARGE-SIGNAL TRANSIENT ANALYSIS

A. Average state trajectory equations

From Fig. 6, it can be seen that the average model of the active-clamp reset circuit is a nonlinear system whose parameters are the functions of the duty cycle. At
the same time, the duty cycle is independent of the parameters of the L_M-C_C resonant network, i.e., it is decoupled from the state variables, v_c and i_m. In addition, since the duty cycle does not change during each switching period, the average model in Fig. 6(b) can be considered linear during each switching period with input voltage fixed at \( \frac{d}{dt} V_{in} \), magnetizing inductance \( L_M \), and clamp capacitance \( C_C \).

By solving (18) and (19), the state trajectory equations during each switching period are

\[
v_c(t) = r(0) \cos[\alpha(0) - \alpha_o \cdot t] + v_{center},
\]

\[
i_m(t) \cdot Z_o = r(0) \sin[\alpha(0) - \alpha_o \cdot t],
\]

where

\[
v_{center} = \frac{d}{dt} V_{in},
\]

\[
r(0) = \sqrt{\left(\sqrt{v_c(0)} - v_{center}\right)^2 + i_m(0)^2 \cdot Z_o^2},
\]

\[
\alpha(0) = \tan^{-1}\left(\frac{i_m(0) \cdot Z_o}{v_c(0) - v_{center}}\right).
\]

In (34) - (38), \( v_c(0) \) is the initial average voltage of the clamp capacitor and \( i_m(0) \) is the initial average magnetizing current of the transformer at the main switch on instant. \( \omega_o = \frac{d}{dt} \frac{1}{\sqrt{L_M \cdot C_C}} \) is the resonant frequency of L_M-C_C resonant network, and \( Z_o = \frac{L_M}{\sqrt{C_C}} \) is the characteristic impedance of the resonant network.

By combining (34) and (35), the state trajectory equation can be written as

\[
\left[ v_c(t) - v_{center}\right]^2 + \left[i_m(t) \cdot Z_o\right]^2 = r(0)^2
\]

It is an eclipse with center \( (v_{center},0) \) in the \( v_c-i_m \) state plane, and a circle in the \( v_c-i_m \cdot Z_o \) state plane. The dynamic equilibrium point, \( v_{center} \), is the center of the state trajectory and is a function of the duty cycle and the input voltage. The average state trajectory is shown in Fig. 9 with the solid line.

Because the duty cycle is a slow varying compared with a switching period, the duty cycle \( d(t) \) changes gradually during transient. Consequently, it can be assumed that the average state trajectory movement is a continuous movement with moving center \( v_{center}(t) \) described by equations (34)-(39), where all quantities dependent on duty cycle are functions of time.

Similarly, one can analyze the average state trajectory in the presence of resistive loss \( R_M \) which represents a sum of the switch on resistance and the core loss of the transformer. The normalized average state trajectory with damping is shown in Fig. 9 with a dashed line. \( v_{center} \) is the spiral point of the state trajectory and the damping of the trajectory is \( e^{-\frac{R_{M,t}}{2L_M}} \).

Since time constant in the damping term is usually very large when no external damping circuit is used, the effect of the damping does not have a significant impact on peak values of state variables in the transient analysis. The rest of the paper will analyze the circuit’s transient behavior without a damping effect.

![Fig. 9. Average state trajectory without damping (solid line); with damping (dashed line).](image)

**B. Movement of the average state trajectory during input-voltage transient**

Before the input-voltage step change from \( V_{in,old} \) to \( V_{in,new} \), the average state trajectory is a single point in the \( v_c-i_m \cdot Z_o \) state plane with duty cycle \( d=D_{old} \). Initial average clamp-capacitor voltage \( v_c(0) = \frac{D_{old}}{D_{old}} \cdot V_{in,old} \), and the average magnetizing current of the transformer \( i_m(0) = 0 \). Since immediately after an input-voltage step change, the duty cycle cannot change instantaneously, the trajectory center after the change is \( v_{center}(0) = \frac{D_{old}}{D_{old}} \cdot V_{in,new} \) and the average state trajectory follows the circle described in (39) with the center \( (v_{center}(0),0) \) and radius \( r(0) = |v_{center}(0) - v_c(0)| \).

When the converter operates with the control loop open, i.e., has a fixed duty cycle, \( d \) does not change. Consequently, \( v_{center} \) and \( r \) do not change, and the state trajectory is a fixed circle as shown in Fig. 10. However, when the forward converter has an output-voltage feedback control, the duty cycle changes gradually from \( D_{old} \) to \( D_{new} \) as described in (32) so the center of the circle moves from \( v_{center}(0) \) to \( v_{center,new} = \frac{D_{new}}{D_{new}} \cdot V_{in,new} \), which is the new steady state value of the clamp-capacitor voltage. The trajectory movement is illustrated in Fig. 11.

Fig. 11(a) and Fig. 11(b) are the state trajectories during input-voltage from 200 V to 300 V transient with a bandwidth \( f_c=3 \) kHz and \( f_c=20 \) kHz, respectively. Both state trajectories follow the open loop circle (dashed line) at the beginning of the transient. Since \( v_{center} \) moves faster in Fig. 11(b) due to a higher bandwidth, the state trajectory in Fig. 11(b) takes less time to move to the new steady state, and it results in a lower peak voltage of the switch and a lower peak magnetizing current (smaller thick solid-line circle).

Fig. 11(c) and Fig. 11(d) are the state trajectories during input-voltage from 300 V to 200 V transient with a bandwidth \( f_c=3 \) kHz and \( f_c=20 \) kHz, respectively. Similar state trajectory movements can be observed. As
can be seen from Fig. 11, the worst case (largest thick solid-line circle) happens when the input-voltage steps from low to high, and the bandwidth is lowest.

The resonant frequency of the active-clamp circuit plays an important role, since the state trajectory is determined by two movements, the state trajectory center movement, whose speed is controlled by the bandwidth $f_s$; and the resonant movement, whose speed is determined by the resonant frequency $f_r$. Fig. 12 shows the calculated maximum values of $v_c$ and $i_m$ as functions of $f_r/f_s$. For the same bandwidth, a lower resonant frequency has a smaller peak clamp-capacitor voltage and peak magnetizing current.

The peak voltage of the main switch and the magnetizing current of the transformer can be calculated by adding the ripple as

$$i_m(peak) = i_m_{ave}(max) + \frac{1}{2} \frac{v_{in}}{L_M} \frac{D \cdot T_s}{(2 \cdot 8 \cdot D_{in} \cdot V_c \cdot T_s^2)}$$

$$v_{st}(peak) = v_{st_{ave}} + v_{st_{ave}}(max) + \frac{1}{2} \cdot \frac{1}{8} \frac{D_{in} \cdot V_c \cdot T_s^2}{L_M \cdot C_c}$$

(40)  

(41)

C. Movement of state trajectory during load transient

Before a load step change, the average state trajectory is a single point in the $v_c - i_m \cdot Z_n$ state plane with duty cycle $d = D_{old}$, initial average clamp-capacitor voltage $v_c(0) = \frac{D_{old}}{D_{old}} \cdot V_{in}$ and the average magnetizing current of the transformer $i_m(0) = 0$. According to (33), at the moment of a step load change, the duty cycle changes for

$$\Delta d = \frac{-n \cdot \omega_r \cdot L_F}{V_{in}} \cdot \Delta I_M,$$

so that the initial trajectory center is

$$v_{center}(0) = \frac{D_{old} + \Delta d}{D_{old} - \Delta d} \cdot V_{in}$$

(42)  

(43)

The average state trajectory follows the circle described in (39) with circle center at $[v_{center}(0), 0]$ and radius $r(0) = |v_{center}(0) - v_c(0)|$.

Because of the output-voltage feedback control, the duty cycle returns gradually to $D_{old}$ as described in (33). Therefore, the center of the circle moves from $v_{center}(0)$ to $v_c(0)$, which is the original steady state value of the clamp-capacitor voltage, as illustrated in Fig. 13.

![Fig. 10. Open-loop state trajectories during input step changes.](image)

Fig. 11. Closed-loop average state trajectories with different bandwidths and input step changes: (a)-(b) input-voltage step from 200 V to 300 V; (c)-(d) input-voltage step from 300 V to 200 V.

![Fig. 12. The maximum average values of $v_c$ and $i_m$ are functions of $f_r/f_s$.](image)

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Fig. 13(a) and Fig. 13(b) are the state trajectories during a step load change from 18 A to 20 A with a bandwidth of $f_s=3$ kHz and $f_s=20$ kHz, respectively. Both state trajectories follow the open loop circle (dashed line) at the beginning of the transient. Since $v_{center}$ moves faster in Fig. 13(b) due to a higher bandwidth, the state trajectory in Fig. 13(b) takes less time to move to the new steady state. It should be noted that according to (33), the circuit with higher control bandwidth has a larger initial duty cycle jump. As a result, the initial radius $r(0)$ is much larger for the high bandwidth case. This is opposite to the case of a step input-voltage change, where the circuit with a higher bandwidth control experiences a larger maximum clamp-capacitor voltage and magnetizing current.

Fig. 13(c) and Fig. 13(d) show the state trajectories during a step load change from 20 A to 18 A with a bandwidth $f_s=3$ kHz and $f_s=20$ kHz, respectively. As can be seen from Fig. 13, the maximum transient voltage stress of the switch and the maximum transient magnetizing current occur for a positive step load change with a high bandwidth. For the same bandwidth, a lower resonant frequency has a smaller peak clamp-capacitor voltage and peak magnetizing current.

In addition, the minimum input-voltage condition exhibits the largest clamp-capacitor voltage and the magnetizing current transient since $v_{center}(0)$ is the largest due to the smallest $d'$. A smaller output-filter inductance helps to reduce the duty cycle change during transients and reduces the peak voltage and the magnetizing current.

VI. SUMMARY

The large-signal transient analysis of the forward converter with the active-clamp reset and the output-voltage feedback control is presented in this paper. Based on the analysis, the circuit performance during large-signal line and load transients can be predicted. It is shown that the ratio of the control bandwidth to resonant frequency is a design parameter of the maximum clamp-capacitor voltage and magnetizing current values. By using this analytical approach, the circuit design issues, such as the switch voltage stress, transformer saturation, and reverse recovery problems in the anti-parallel diode of the active-clamp switch can be addressed.

REFERENCES