

# Universal-Input Single-Stage PFC Flyback with Variable Boost Inductance for High-Brightness LED Applications

Yuequan Hu, Laszlo Huber, and Milan M. Jovanović

Delta Power Electronics Laboratory  
Delta Products Corporation  
P.O. Box 12173, 5101 Davis Drive  
Research Triangle Park, NC 27709, USA  
Email: yhu@deltartp.com

**Abstract** — This paper presents a single-stage flyback power-factor-correction circuit with a variable boost inductance for high-brightness light-emitting-diode applications for the universal input voltage (90-270 V<sub>rms</sub>). The proposed circuit overcomes the limitations of the conventional single-stage PFC flyback with a constant boost inductance, which cannot be designed to achieve a practical bulk-capacitor voltage level (i.e., less than 450 V) at high line while meeting the IEC 61000-3-2 Class C line current harmonic limits at low line. According to the proposed variable boost inductance method, the boost inductance is constant in the high-voltage range and it is reduced in the low-voltage range, resulting in discontinuous-conduction-mode operation and a low total harmonic distortion (THD) in both the high-voltage and low-voltage ranges. Measurements obtained on a 24-V/91-W experimental prototype are as follows: PF = 0.9873, THD = 12%, and efficiency = 88% at nominal low line (120 V<sub>rms</sub>); and PF = 0.9474, THD = 10.39%, and efficiency = 91% at nominal high line (230 V<sub>rms</sub>). The line current harmonics satisfy the IEC 61000-3-2 Class C limits with enough margin.

## I. INTRODUCTION

The technology and performance of high-brightness light-emitting diodes (HB LEDs) has undergone significant improvements driven by new applications in liquid-crystal-display (LCD) backlighting, automobiles, traffic lights, and general-purpose lighting [1]-[3]. As a solid state light source which does not contain mercury, HB LEDs have been widely accepted because of their superior longevity, low-maintenance requirements, and continuously-improving luminance with a great potential to replace existing lighting sources such as incandescent and fluorescent lamps in the future.

For LED drivers with an output power over 25 W in general lighting applications, the line current harmonics have to satisfy the limits set by IEC 61000-3-2 Class C regulations [4]. With passive power-factor-correction (PFC), which uses only inductors and capacitors, it is difficult to meet such requirements, and the size of the components is large.

An LED driver with active PFC, which is implemented with two stages, is shown in Fig. 1. The first stage can

achieve a near unity power factor and a low THD at the universal input voltage, while the second stage is used for the dc/dc conversion. However, the circuit in Fig. 1 requires two independently controlled power switches and two control circuits, leading to a high component count, increased cost, and larger size. In low-power lighting applications, where cost is the dominant issue, such an approach loses appeal.

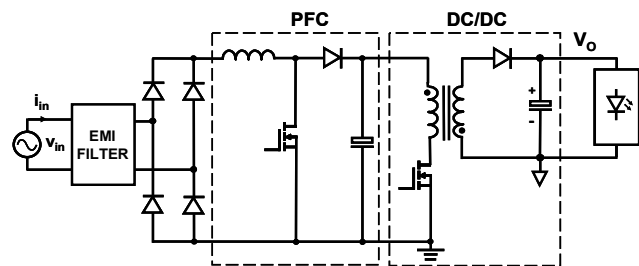


Fig. 1. Conventional two-stage LED driver.

Another active PFC implementation employs a single-stage ac/dc converter [5]-[13], where the PFC stage is integrated with the dc/dc stage, resulting in a reduced complexity and cost. The single-stage PFC ac/dc converter can be implemented without and with a bulk capacitor at the primary side, as illustrated in Figs. 2 and 3, respectively. Although the single-stage PFC circuit in Fig. 2 [5] has the advantage of a low component count, its output voltage has a high ripple at twice the line frequency unless very large output capacitors are used. For an LED load, a small variation in the driving voltage can lead to a large variation in the LED current. A large ripple of the LED current would seriously affect the longevity of the LEDs [12]. Therefore, the approach in Fig. 2 often requires a post-regulator, which adds cost and lowers the efficiency.

The single-stage PFC flyback topology shown in Fig. 3 [11] presents one of the most cost-effective single-stage solutions. In this converter, the PFC stage operates in discontinuous conduction mode (DCM), while the dc/dc stage operates at the DCM/CCM (continuous-conduction-mode) boundary. A low input-current harmonic distortion

can be achieved due to the inherent property of the DCM boost converter to draw a near sinusoidal current if its duty cycle is held relatively constant during a half line cycle. However, voltage  $V_B$  across bulk capacitor  $C_B$  is not regulated and at high line it can increase to impractical levels. To reduce the bulk capacitor voltage, one terminal of the boost inductor winding is connected to a tapping point of the primary winding of the flyback transformer, which provides a negative magnetic feedback [7]. However, the tapping of the flyback primary winding also results in a zero-crossing distortion of the line current. In fact, as long as the instantaneous line voltage is lower than the voltage at the tapping point, no current is drawn from the input, which reduces the power factor and increases the line-current harmonics.

The single-stage PFC flyback topology shown in Fig. 3 has been successfully applied in adapter/charger applications for the universal line voltage, where the line current harmonics need to meet the IEC 61000-3-2 Class D limits, which are less stringent than the IEC 61000-3-2 Class C limits.

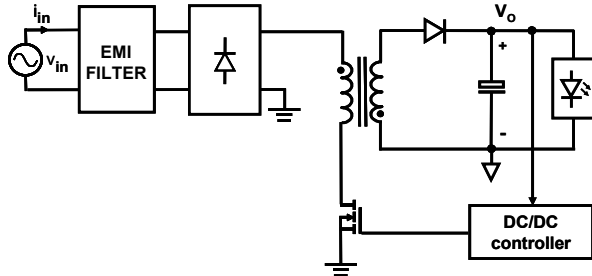


Fig. 2. Single-stage flyback LED driver without energy-storage capacitor at primary side.

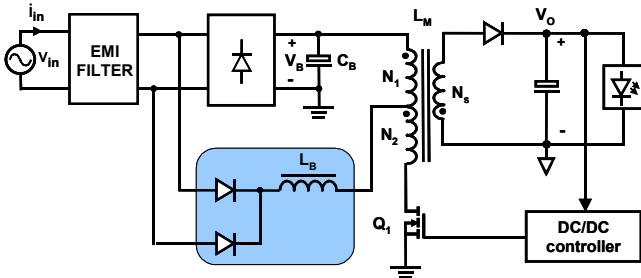


Fig. 3. Single-stage flyback LED driver with energy-storage capacitor at primary side.

It was shown in [14] that the single-stage PFC flyback in Fig. 3 with a constant boost inductance cannot be designed to achieve a practical bulk-capacitor voltage level (i.e., less than 450 V) at high line while meeting the IEC 61000-3-2 Class C line-current harmonic limits at low line. To overcome these limitations, a variable boost inductance is required, i.e., a high boost inductance at high line to limit the bulk-capacitor voltage and a lower boost inductance at low line to ensure DCM operation and a low THD. In fact, at low line, when a constant boost inductance is used, the inductor will enter CCM operation around the peak of the line voltage, and the

line current waveform will have a bulge around its peak value [14], resulting in an increased THD. Furthermore, if the bulk-capacitor voltage is slightly lower than the peak of the rectified line voltage, the peak charging of the bulk capacitor through the bridge rectifier will also result in a bulge in the line current waveform [7] with an increased THD.

In this paper, it is shown that by optimizing the tapping point of the primary-winding of the flyback transformer in Fig. 3 and by employing a novel technique to reduce the boost inductance at low line, a high power factor and a low THD with relatively high efficiency can be achieved such that the line current harmonics satisfy the IEC 61000-3-2 Class C limits.

## II. VARIABLE BOOST INDUCTANCE

### A. Concept

As voltage  $V_B$  across bulk-capacitor  $C_B$  in Fig. 3 is not regulated and varies with both the input voltage and output power, the design of the magnetic components significantly affects the bulk-capacitor voltage level. Generally, a higher boost inductance  $L_B$  leads to a lower voltage  $V_B$ . If the boost inductance increases during steady-state operation, the input power initially decreases because of a lower input current. The difference between the output power and input power has to be supplied from the bulk capacitor, causing a drop of the bulk-capacitor voltage. Meanwhile, as the bulk-capacitor voltage decreases, the duty cycle of main switch  $Q_1$  increases to keep the output voltage regulated, resulting in an increase of the input power until a new balance between the input and output power is reached. A higher boost inductance can limit voltage  $V_B$  to an acceptable level and ensure DCM operation at high line. However, at low line, if the boost inductance is larger than the maximum value for DCM operation, the boost inductor will operate in CCM around the peak of the rectified line voltage, resulting in a severe distortion of the line current [14]. Therefore, a variable boost inductance is required, i.e., a high boost inductance at high line and a lower boost inductance at low line.

Various methods for achieving a variable inductance were reported in [15]-[23], but their applications are limited either because of a high power loss [15]-[20], or complexity of the implementation [21]-[22], or because they can only meet IEC 61000-3-2 Class D current harmonic limits [23].

The concept of the variable boost inductance proposed in this paper is shown in Fig. 4. The basic PFC boost inductor is implemented with an EE core and winding  $N_{LB}$ . A half core (E) with winding  $N_{BIAS}$  is closely attached to the bottom part of the EE core. The boost inductance  $L_B$  is controlled by a bias current  $I_{BIAS}$ . The control circuit includes switch  $Q_{BIAS}$ , a dc bias control circuit, and an input voltage sensing circuit. At low line, switch  $Q_{BIAS}$  is open by sensing the input voltage, and the bias current flows through bias winding  $N_{BIAS}$ , inducing a magnetic flux  $\Phi_{BIAS}$  that is added to the main magnetic flux  $\Phi_{LB}$  at the bottom part of the boost-inductor EE core. As a result, at the bottom part of the EE core, the effective permeability is reduced, and consequently, the boost

inductance is decreased [17]. The reduction of the boost inductance is proportional to the applied bias current. At high line, switch  $Q_{BIAS}$  is closed, shorting bias winding  $N_{BIAS}$ . As a result, there is no bias current through winding  $N_{BIAS}$ , and the boost inductance does not change.

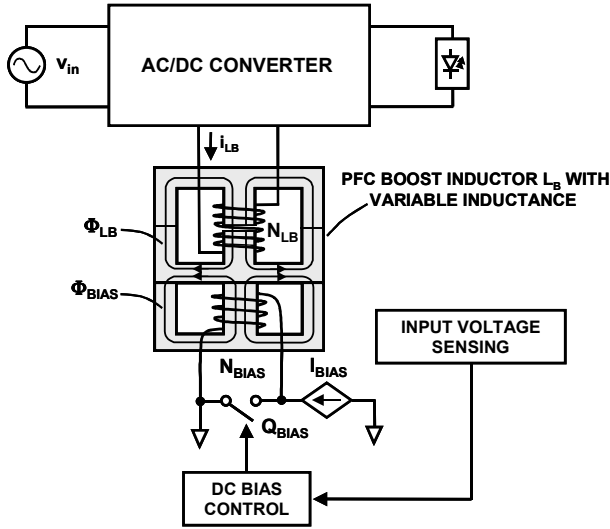


Fig. 4. Concept of proposed single-stage PFC with a variable boost inductance.

### B. Control circuit

Figure 5 shows the detailed schematic of the proposed single-stage PFC flyback HB LED driver. The input voltage is sensed by a circuit comprising winding  $N_3$  wound around the boost-inductor EE core, diode  $D_8$ , and capacitor  $C_1$ . The load current is used as the dc bias current to reduce complexity and loss of efficiency. Switch  $Q_2$  connected in series with the LED load is the bias switch  $Q_{BIAS}$  in Fig. 4.

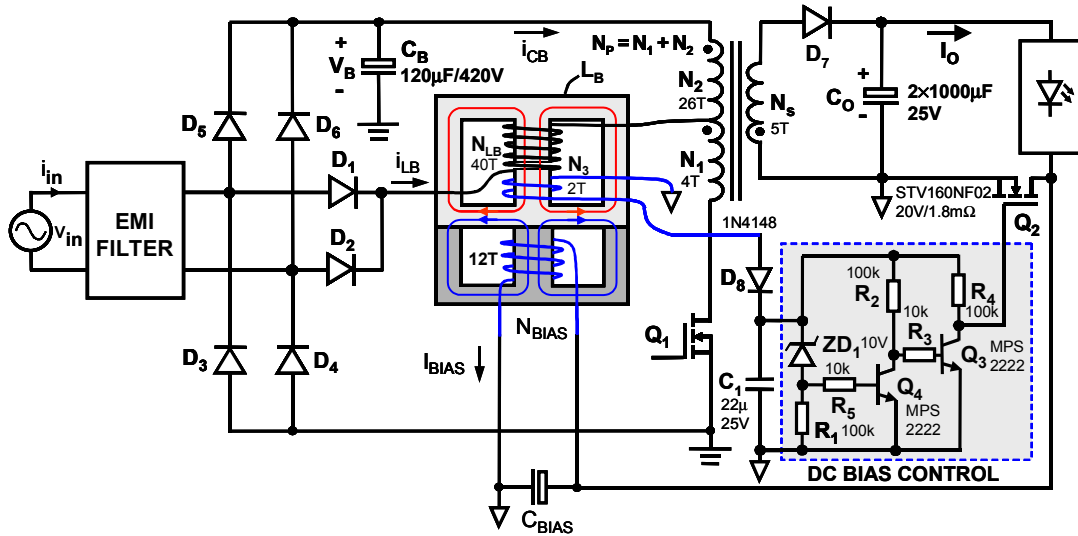


Fig. 5. Schematic of proposed single-stage PFC flyback with a variable boost inductance for HB LED applications.

When main switch  $Q_1$  is turned on, diode  $D_8$  is forward biased, peak charging capacitor  $C_1$  with a maximum voltage

$$V_{C1MAX} = (\sqrt{2}V_{IN} - \frac{N_1}{N_p} V_B) \frac{N_3}{N_{LB}}, \quad (1)$$

where  $N_1$ ,  $N_p$  and  $N_{LB}$  are the number of turns of the feedback winding, primary winding of the flyback transformer, and the boost-inductor winding, respectively. A proper turns number  $N_3$  is chosen so that the voltage across capacitor  $C_1$  turns on Zener diode  $ZD_1$  only at high line (180-270 Vrms). When  $ZD_1$  is turned on, switch  $Q_4$  is turned on and switch  $Q_3$  is turned off. As a result, the gate-to-source voltage of MOSFET  $Q_2$  is high and  $Q_2$  is turned on. The load current flows through switch  $Q_2$  and the bias current of bias winding  $N_{BIAS}$  is approximately zero. Therefore, the boost inductance remains unchanged. It should be noted that the turn-on resistance of switch  $Q_2$  needs to be negligible compared to the resistance of bias winding  $N_{BIAS}$  to prevent a substantial current flowing through the bias winding at high line. Otherwise, the effective boost inductance would become lower and voltage  $V_B$  would increase to an undesirable level. At low line, the voltage across capacitor  $C_1$  is lower than the turn-on voltage of  $ZD_1$ ,  $Q_4$  is turned off and  $Q_3$  is turned on. As a result, the gate-to-source voltage of MOSFET  $Q_2$  is low and  $Q_2$  is turned off. The entire load current flows through the bias winding. Therefore, the boost inductance is reduced.

### C. Design considerations

The design of the flyback circuit in Fig. 5 without the PFC part is the same as the design of the conventional flyback circuit. Key design parameters of the PFC part of the flyback circuit in Fig. 5 are number of turns  $N_1$  and boost inductance  $L_B$ . The design goal is to achieve a proper PFC operation, i.e., the line current to meet the IEC 61000-3-2 Class C limits, and to limit bulk-capacitor voltage  $V_B$  below 400 V.

It was shown in [14] that bulk-capacitor voltage  $V_B$  is a function of input voltage  $v_{IN}$ , ratio of inductances  $L_B/L_M$ , ratio of number of turns  $N_1/N_p$ , and output voltage  $V_o$ , i.e.,

$$V_B = f(v_{IN}, L_B/L_M, N_1/N_p, V_o). \quad (2)$$

The bulk-capacitor voltage increases with increasing rms value of the line voltage, and it decreases with increasing turns ratio  $N_1/N_p$  and increasing ratio of inductances  $L_B/L_M$ , as illustrated in Figs. 6 and 7, respectively.

For proper PFC operation, in order to meet the IEC 61000-3-2 Class C limits, the zero-crossing distortion of the line current due to the tapping of the primary winding should be optimized, and the boost inductor should be prevented from operating in CCM.

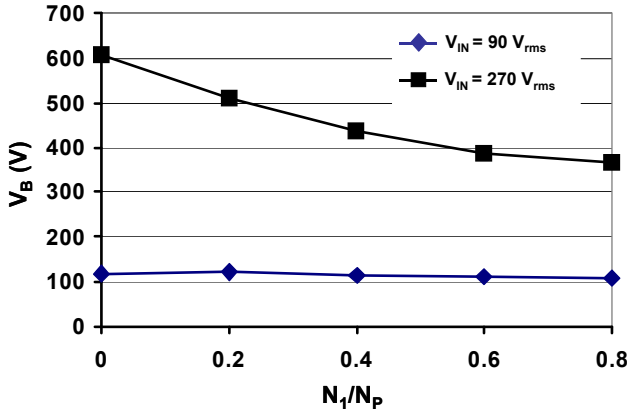


Fig. 6. Calculated voltage  $V_B$  vs. ratio  $N_1/N_p$  ( $L_B/L_M=0.25$ ).

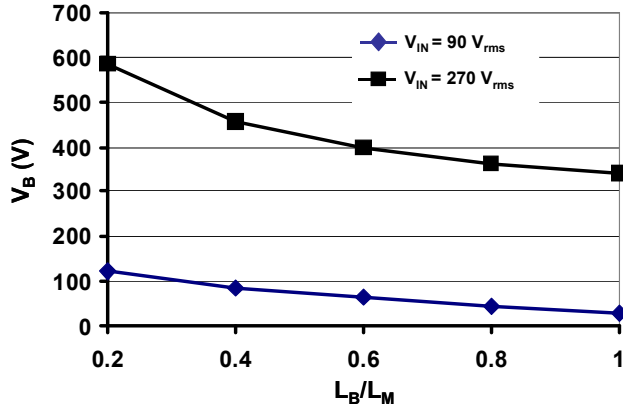


Fig. 7. Calculated voltage  $V_B$  vs. ratio  $L_B/L_M$  ( $N_1/N_p=0.133$ ).

Following the same procedure for the analysis of the bulk-capacitor voltage as in [14] and assuming that the boost inductor operates in DCM, the line current waveform and the corresponding THD can be easily calculated. For example, calculated line current waveforms at three different turns ratios  $N_1/N_p$ , at nominal low line ( $V_{IN} = 120$  Vrms), are shown in Fig. 8. It follows from Fig. 8 that with increasing turns ratio  $N_1/N_p$  the dead-angle of the line current around zero crossing increases, resulting in an increased THD. As another example, Fig. 9 shows calculated THD vs.  $N_1/N_p$  for three different values of  $L_B$ , at nominal high line ( $V_{IN} = 230$

Vrms). It follows from Fig. 9 that THD significantly increases with increasing  $N_1/N_p$ , whereas the presented variation of  $L_B$  does not have significant effect on THD. It can be seen in Fig. 9 that for a THD lower than 20%, which is a typical requirement for lighting applications, turns ratio  $N_1/N_p$  should be smaller than 0.15.

In order to ensure DCM operation of boost inductor  $L_B$ , time  $T_{RES\_LB}$ , i.e., the time to completely reset the boost-inductor core, should be shorter than the turn-off time,  $T_{OFF\_Q1}$ , of switch  $Q_1$  around the peak of the line voltage (worst case), i.e.,

$$T_{RES\_LB} \leq T_{OFF\_Q1}. \quad (3)$$

In this way, the current flowing through the boost inductor decreases to zero before switch  $Q_1$  is turned on, ensuring a high power factor and a low THD.

The turn-off time,  $T_{OFF\_Q1}$ , of switch  $Q_1$  operating at CCM/DCM boundary can be expressed as

$$T_{OFF\_Q1} = \left(1 - \frac{V_o N_p / N_s}{V_B + V_o N_p / N_s}\right) T_s, \quad (4)$$

where,  $T_s$  is the switching period of switch  $Q_1$ .

The time to completely reset the boost-inductor core can be expressed as

$$T_{RES\_LB} = \frac{(v_{IN}^{rec} - N_1 V_B / N_p) N_p V_o / N_s}{[V_B + (1 - N_1 / N_p) N_p V_o / N_s - v_{IN}^{rec}] (V_B + N_p V_o / N_s)} T_s, \quad (5)$$

where,  $v_{IN}^{rec}$  is the instantaneous rectified line voltage.

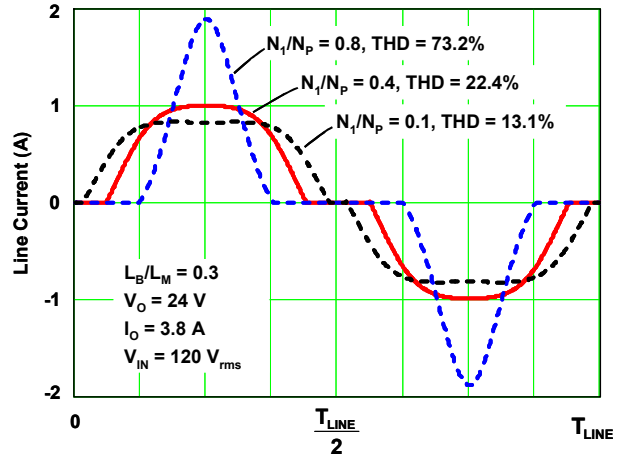


Fig. 8. Calculated line current waveforms for different ratios of  $N_1/N_p$ .

Using (2)-(5), the maximum ratio  $L_B/L_M$  vs.  $N_1/N_p$  that will ensure operation of  $L_B$  in DCM can be calculated. In Fig. 10, the calculated maximum ratio  $L_B/L_M$  vs.  $N_1/N_p$  that will ensure operation of  $L_B$  in DCM is presented at nominal low line (120 Vrms). Figure 10 also includes the calculated minimum  $L_B/L_M$  vs.  $N_1/N_p$  that will ensure limiting the bulk-capacitor voltage below 400 V at the upper end of the low line-voltage range (140 Vrms).

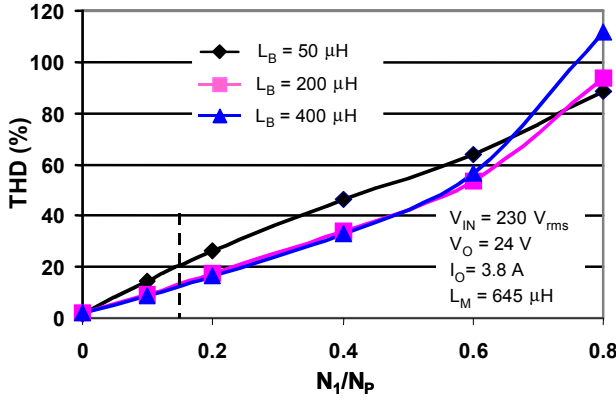


Fig. 9. Calculated THD vs. ratio  $N_1/N_p$  at  $V_{IN} = 230$  Vrms.

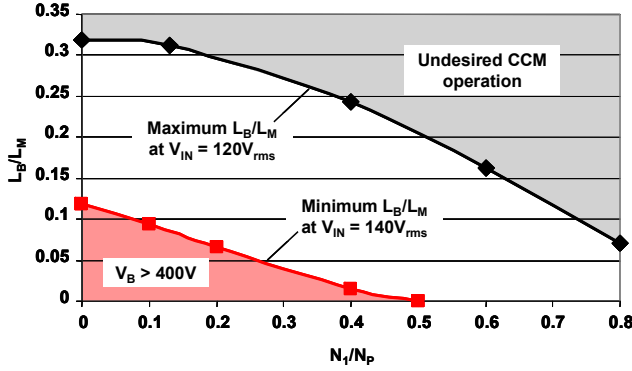


Fig. 10. Desired range for ratio  $L_B/L_M$  vs. ratio  $N_1/N_p$  in the low line-voltage range.

The calculated maximum and minimum ratios  $L_B/L_M$  vs.  $N_1/N_p$  in the high line-voltage range are presented in Fig. 11. As follows from Fig. 11, in the high line-voltage range, the possible range of ratio  $L_B/L_M$  is much narrower than at the low line-voltage range. It also follows from Fig. 11 that the minimum possible turns ratio  $N_1/N_p$  is 0.1.

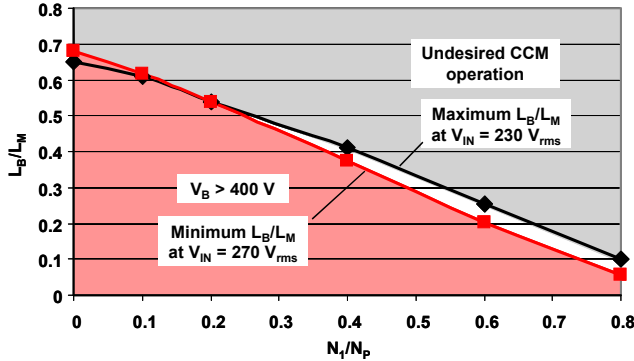


Fig. 11. Desired range for ratio  $L_B/L_M$  vs. ratio  $N_1/N_p$  in the high line-voltage range.

It can be clearly seen from Figs. 10 and 11 that different ratios of inductances  $L_B/L_M$  are required in the low line-voltage range and in the high line-voltage range, i.e., that a variable boost inductance is required in the universal line-voltage range.

Based on the calculated results presented in Figs. 6-9, turns ratio  $N_1/N_p = 0.13$  ( $N_1 = 4$ ,  $N_p = 30$ ) is selected for the

final design. It follows from Fig. 11 that for  $N_1/N_p = 0.13$  in the high line-voltage range, ratio  $L_B/L_M$  should be around 0.6, i.e., the desired boost inductance is 390 uH for the selected  $L_M = 645$  uH.

Finally, it follows from Fig. 10 that for  $N_1/N_p = 0.13$  in the low line-voltage range, ratio  $L_B/L_M$  should be smaller than 0.32, i.e., the desired boost inductance should be smaller than 206 uH for the selected  $L_M = 645$  uH.

### III. EXPERIMENTAL RESULTS

To verify the proposed variable boost-inductance technique, a 24-V/91-W single-stage PFC flyback prototype for HB LED applications was built. Figure 12 shows a photograph of the variable boost inductor with a dc bias winding, while Fig. 13 shows the measured boost inductance vs. dc bias current. As shown in Fig. 13, the effective boost inductance drops faster with increasing dc bias current when the turns number  $N_{BIAS}$  of the bias winding is higher, and therefore, it requires a lower dc bias current. However, a higher turns number  $N_{BIAS}$  leads to a higher resistance, hence, higher winding loss for the same load current. Moreover, a lower boost inductance generally results in a lower overall efficiency of the LED driver. Therefore, turns number  $N_{BIAS}$  should be minimized to ensure low-enough boost inductance and DCM operation at low line while maintaining relatively high efficiency. A turns number  $N_{BIAS}$  of 12 was selected for the final design. The dc resistance of winding  $N_{BIAS}$  is 20 m $\Omega$  while the turn-on resistance of bias control switch  $Q_2$  is 1.8 m $\Omega$  ( $\ll 20$  m $\Omega$ ). At low line, switch  $Q_2$  is turned off, and the entire load current  $I_O = 3.8$  A flows through the bias winding resulting in a power loss of 0.29 W, i.e., a 0.3% decrease of efficiency. At high line, bias switch  $Q_2$  is turned on and bias winding  $N_{BIAS}$  is essentially shorted since its dc resistance is much higher than the turn-on resistance of switch  $Q_2$ , resulting in a power loss of 22 mW at  $I_O = 3.8$  A.

The measured line voltage and line current waveforms at full load are shown in Fig. 14. At nominal high line (230 Vrms), THD = 10.39%, PF = 0.9474,  $V_B = 327$  V, and efficiency = 91%; while at nominal low line (120 Vrms), THD = 12.24%, PF = 0.9873,  $V_B = 193$  V, and efficiency = 88% were obtained. Figure 15 shows that the measured line-current harmonics are below the IEC 61000-3-2 Class C limits with enough margin. The measured efficiency vs. output power is shown in Fig. 16.

Measurements with an actual LED load were also performed. Four LED strings each with 7 series-connected white LEDs (Philips Lumileds, LXHL-LW3C) were paralleled and directly driven by the proposed PFC flyback prototype with an output voltage of 24 V. The measured LED current and output voltage ripple are shown in Fig. 17. The peak-to-peak output voltage ripple is 30 mV, resulting in a low LED current ripple (1.6% of the average current). Therefore, the proposed PFC flyback circuit is suitable for directly driving LED strings, and no post-regulators are necessary, which is a significant advantage over the conventional PFC flyback circuit without an energy-storage capacitor at the primary side.

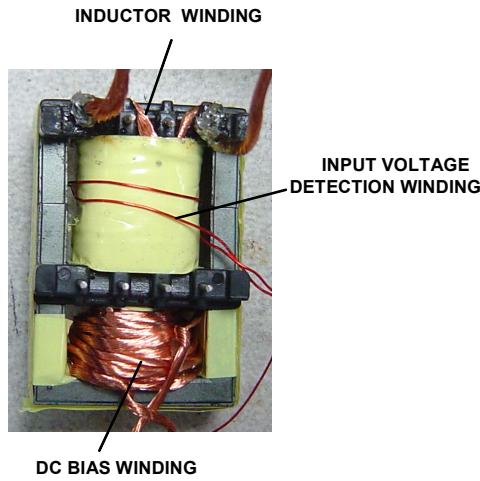


Fig. 12. Photograph of the variable boost inductor.

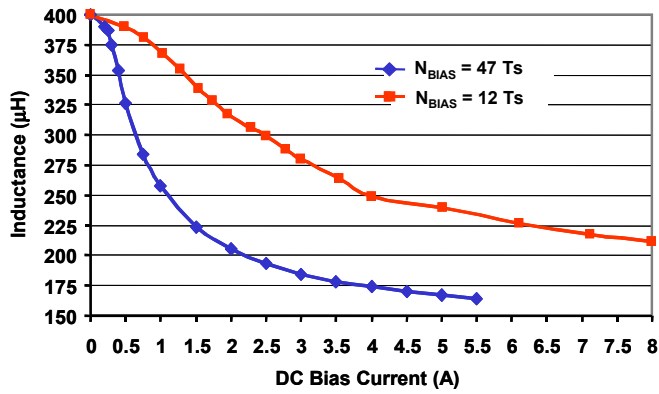
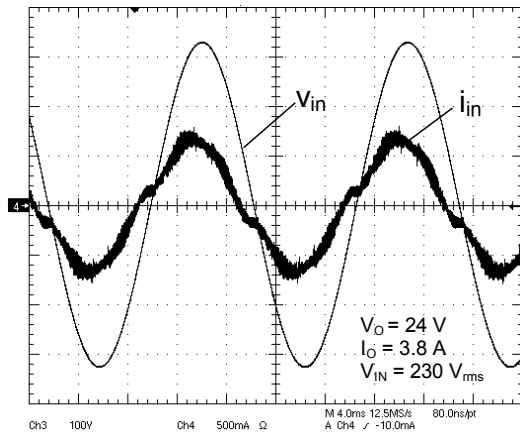
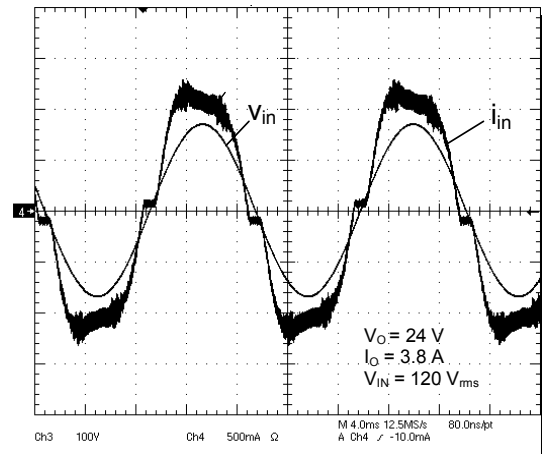


Fig. 13. Measured boost inductance vs. dc bias current.



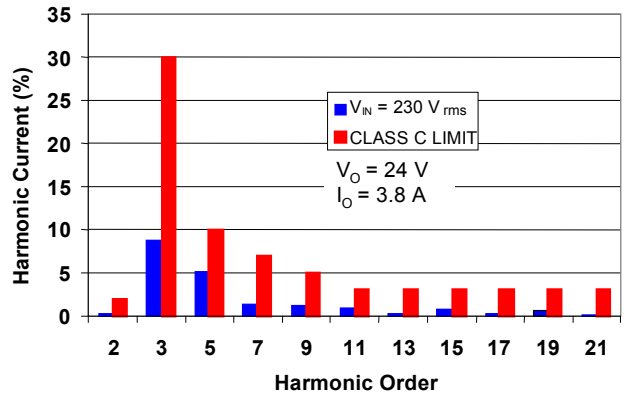
Error!

(a)

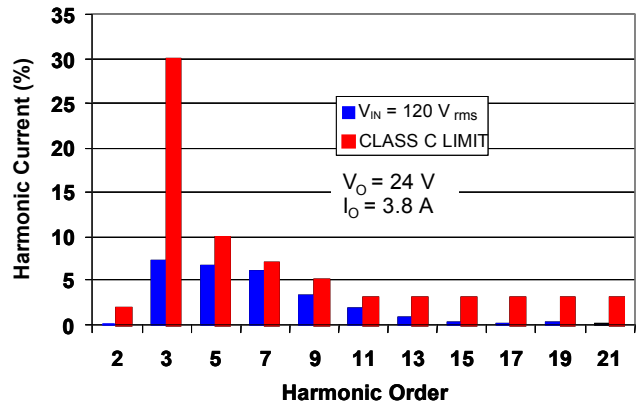


(b)

Fig. 14. Measured line current (500 mA/div.) and line voltage (100 V/div.) waveforms, (a)  $V_{IN} = 230$  V<sub>rms</sub>; (b)  $V_{IN} = 120$  V<sub>rms</sub>.



(a)



(b)

Fig. 15. Measured line current harmonics, (a)  $V_{IN} = 230$  V<sub>rms</sub>; (b)  $V_{IN} = 120$  V<sub>rms</sub>.

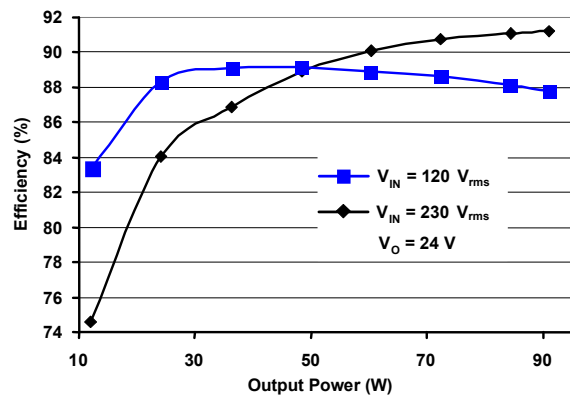


Fig. 16. Measured efficiency vs. output power.

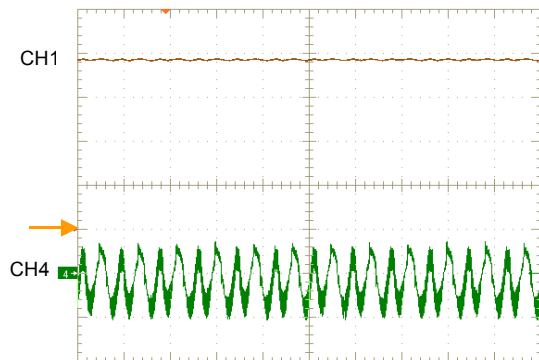


Fig. 17. Measured LED current and output voltage ripple at  $V_{IN} = 230 \text{ V}_{rms}$ . CH1: LED current (1 A/div.); CH4: Output voltage ripple (20 mV/div.); Time scale: 10 ms/div.

#### IV. SUMMARY

A single-stage PFC flyback with a variable boost inductance for HB LED applications for the universal input voltage is presented in this paper. Experimental results obtained on a 24-V/91-W prototype show that the proposed PFC converter achieves an efficiency of 88%, a power factor of 0.9873 and a THD of 12.24% at nominal low line (120 Vrms), and an efficiency of 91%, a power factor of 0.9474 and a THD of 10.39% at nominal high line (230 Vrms). Line-current harmonics satisfy the IEC 61000-3-2 Class C limits with enough margin.

#### REFERENCES

[1] J. Y. Tsao, "Solid-state lighting: lamps, chips, and materials for tomorrow," *IEEE Circuits and Devices Magazine*, vol. 20, no. 3, pp. 28 - 37, May-June 2004.

[2] N. Narendran and Y. Gu, "Life of LED-based white light sources," *Journal of Display Technology*, vol. 1, no. 1, pp. 167 - 171, Sept. 2005.

[3] T. Komine and M. Nakagawa, "Fundamental analysis for visible-light communication system using LED lights," *IEEE Trans. on Consumer Electronics*, vol. 50, no. 1, pp. 100 - 107, Feb. 2004.

[4] Electromagnetic Compatibility (EMC), Part 3-2: Limits-Limits for harmonic current emissions (equipment input current  $\leq 16 \text{ A}$  per phase), International Standard IEC 61000-3-2, 2001.

[5] ON Semiconductor, "90 W, universal input, single stage, PFC converter," [www.onsemi.com/pub\\_link/Collateral/AND8124-D.PDF](http://www.onsemi.com/pub_link/Collateral/AND8124-D.PDF), Dec. 2003.

[6] R. Redl, L. Balogh, and N. O. Sokal, "A new family of single-stage isolated power-factor correctors with fast regulation of the output voltage," *Proc. IEEE Power Electronics Specialists Conf.*, 1994, pp.1137-1144.

[7] L. Huber and M. M. Jovanovic, "Single-stage single-switch input-current-shaping technique with reduced switching loss," *IEEE Trans. Power Electron.*, vol. 15, no. 4, pp. 681-687, July 2000.

[8] C. Qiao and K. M. Smedley, "A topology survey of single-stage power factor corrector with a boost type input-current-shaper," *IEEE Trans. Power Electron.*, vol. 16, no. 3, pp. 360-368, May 2001.

[9] Q. Zhao, F. C. Lee, and F. Tsai, "Voltage and current stress reduction in single-stage power factor correction ac/dc converters with bulk capacitor voltage feedback," *IEEE Trans. Power Electron.*, vol. 17, no. 4, pp. 477 - 483, July 2002.

[10] G. Spiazzi, S. Buso and G. Meneghesso, "Analysis of a high-power-factor electronic ballast for high brightness light emitting diodes," *IEEE Power Electronics Specialists Conference (PESC) Proc.*, pp. 1494 - 1499, 11 - 14 Sept. 2005.

[11] L. Huber and M. M. Jovanovic, "AC/DC flyback converter," U. S. Patent No. 6950319, Sept. 2005.

[12] T. F. Pan, H. J. Chiu, S. J. Cheng, and S. Y. Chyng, "An improved single-stage PFC flyback converter for high-luminance lighting LED lamps," *The 8th International Conference on Electronic Measurement and Instruments*, vol. 4, pp. 212 - 215, Aug. 2007.

[13] K. Zhou, J. G. Zhang, and S. Yuvarajan, "Quasi-active power factor correction circuit for HB LED driver," *IEEE Trans. on Power Electron.*, vol. 23, no. 3, pp. 1410 - 1415, May 2008.

[14] Y. Hu, L. Huber and M. M. Jovanovic, "Single-stage flyback power-factor-correction front-end for HB LED application," *Proc. of IAS 2009*, Oct. 2009.

[15] C. A. Willis, "Ballast control device," U.S. Patent No.3,873,910, Mar. 25, 1975.

[16] R. T. Elms, "Variable inductance ballast apparatus for HID lamp," U.S. Patent No. 4,162,428, July 24, 1979.

[17] S. F. Lim and A. M. Khambadkone, "Non linear inductor design for improving light load efficiency of boost PFC," *IEEE ECCE 2009 Proceedings*, pp. 1339 - 1346, 2009.

[18] S. B. Yaakov and M. M. Peretz, "A self-adjusting sinusoidal power source suitable for driving capacitive loads," *IEEE Trans. on Power Electron.*, vol. 21, no.4, pp. 890 - 898, July 2006.

[19] D. Medini and S. B. Yaakov, "A current-controlled variable-inductor for high frequency resonant power circuits," *Conference Proceedings of Applied Power Electronics Conference and Exposition*, vol. 1, pp. 219-225, 1994.

[20] C. Q. Lee, K. Siri, A. K. Upadhyay, "Parallel resonant converter with zero voltage switching," U. S. Patent No. 4,992,919, Dec. 1991.

[21] R. E. Hammond, E. F. Rynne, and L. J. Johnson, "Voltage controlled variable inductor," U. S. Patent 5,999,077, Dec. 7, 1999.

[22] G. Roberge and A. Doyon, "Variable inductor," U.S. Patent No. 4,393,157, July 12, 1983.

[23] W. H. Wölfle and W. G. Hurley, "Quasi-active power factor correction with a variable inductive filter: theory, design and practice," *IEEE Trans. on Power Electron.*, vol. 18, no.1, PP. 248-255, Jan. 2003.